



## Results and future work

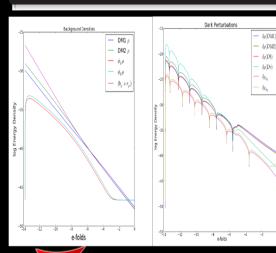
- Forthcoming paper to present these results in full, with maps of stable regions of couplings parameter space, and release PYESSENCE code for community
- Constrain models through stability
- Constrain models through comparison with LSS surveys (Euclid etc.)

#### Why Coupled Quintessence?

- $\bullet$  Late time accelerated expansion simplest solution: Cosmological Constant,  $\Lambda$  "Dark Energy?" problems e.g. coincidence
- Alternatives: one or more scalar fields
- Coupled Quintessence: Canonical scalar field(s),  $\phi$ , with potential  $V(\phi)$ , interacting gravitationally with all components, and through couplings between DE and CDM components solves problems e.g. coincidence (Quintessence alone), breaking tracking (when Coupled)
- Potential examples: Exponential, $V_0e^{-\lambda\kappa\phi}$ , Freezing, e.g.  $M^{4-n}\phi^{-n},(n>0)$ , Thawing, e.g.  $M^4\cos^2(\frac{\phi}{\ell})$ , etc., a "potential" glut

# Work to date

• For first time plotted evolution of stable perturbations to this 2 fluid, 2 field, sum of exponentials model, for a point in coupling constant space, in fourier space. For the plot below  $k=H_{\rm 0}$ 



# Beyond Lambda:

Numerical Problems in Perturbed Coupled Quintessence Alex Leithes\*

## Ouestions of Coupled Ouintessence

- Need a generalised code to test any given coupled quintessence model and allow comparison with observations
- We are developing code, PYESSENCE, to do this
- Background evolution of a model must match observations (CMB, SN data)
- If background satisfies this, is the perturbed model stable (under what range of couplings/ no. of fields etc.)?
- If perturbation are stable do they match observations from large scale structure surveys e.g. BOSS, DES, eBOSS, DESI, Euclid?

## The key equations

- We perturbed around flat FLRW
- We derived the perturbed equations for multiple CDM fluids and DE fields for first time in full generality, gauge unspecified, allowing for pressure (c.f. 1407.2156 Amendola, Barreiro, Nunes for earlier work)
- Allows us to write completely general code for the community to test wide range of models under differing conditions
- Finished code will also allow different selections of gauge

#### Work to date

- Code designed to step through parameter space of couplings, slopes of potentials, determine region of parameter space for stable perturbations
- First implementation longitudinal gauge
- ullet Code to be used for N fields, M fluids
- Initial testing for 2 fields and 2 fluids
- Also for testing, sum of exponential potential chosen

$$V(\phi_1...\phi_n) = M^4 \sum e^{-\kappa \lambda_I \phi_I}$$

(gives analytical solution for background evolution)

### The key equations

Perturbed metric,

$$ds^{2} = -(1+2\Phi)dt^{2} + 2aB_{,i}dtdx^{i} + a^{2}(\delta_{ij} + 2C_{ij})dx^{i}dx^{j}$$

Conservation equation:

$$\begin{split} & \delta \dot{\rho}_{\alpha} + \left(\frac{\nabla^{2} v_{\alpha}}{a} + \dot{E} - 3\dot{\psi}\right) (\bar{\rho}_{\alpha} + \bar{P}_{\alpha}) + 3H(\delta \rho_{\alpha} + \delta P_{\alpha}) = \\ & - \kappa \sum_{I} \mathbb{C}_{I\alpha} (\bar{\rho}_{\alpha} - 3\bar{P}_{\alpha}) \dot{\delta} \dot{\phi}_{I} - \kappa \sum_{I} \mathbb{C}_{I\alpha} (\delta \rho_{\alpha} - 3\delta P_{\alpha}) \dot{\bar{\phi}}_{I} \end{split}$$

Field perturbations:

$$\begin{array}{l} \ddot{\delta\phi}_I + 3H\dot{\delta\phi}_I + V''\delta\phi_I + (\dot{E} - 3\dot{\psi})\dot{\bar{\phi}}_I + \frac{k^2}{a^2}\delta\phi_I + \frac{\dot{\bar{\phi}}_I}{a}k^2B - \dot{\bar{\phi}}_I\dot{\Phi} + \\ 2V'\Phi - 2\kappa\sum\limits_{\alpha}\mathbb{C}_{I\alpha}(\bar{\rho} - 3\bar{P})\Phi - \kappa\sum\limits_{\alpha}\mathbb{C}_{I\alpha}(\delta\rho - 3\delta P) = 0 \end{array}$$

Einstein Field Equations also derived