

Exotic mesons in a holographic approach to QCD

L. Bellantuono, P. Colangelo, F. Giannuzzi

Università degli Studi di Bari, INFN Bari

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QCD describes strong interactions among quarks as processes with colored self-interacting gluons exchanged. This picture brings to the prediction of hybrid bound states with gluons appearing as constituents. Hybrid mesons are configurations composed by a quark, an antiquark and an excited gluon, which accounts for either ordinary or exotic J^{PC} quantum numbers. Mesons with exotic quantum numbers cannot be described as simple quark-antiquark pairs, so their detection would demonstrate the existence of non-standard structures comprising gluons as constituents. Several QCD models indicate the hybrid meson with quantum numbers $J^{PC}=1^{-+}$ as the lowest-lying exotic state. In the light quark sector there are at least three quite well established hybrid candidates: the $\pi_1(1400)$ and the $\pi_1(1600)$, observed in diffractive $\pi^- N$ reactions and $\bar{p} N$ annihilation, and the $\pi_1(2015)$, seen only in diffraction.

Soft-Wall AdS/QCD

SUPER-YANG-MILLS (SYM)
theory on Minkowski space \mathcal{M}_4

- Coupling constant g_{YM}
- $N=4$ SUSY generators
- Gauge group $SU(N)_{\text{color}}$

Strong-coupling limit

$$N \rightarrow \infty, \lambda = g_{YM}^2 N \rightarrow \infty, g_{YM}^2 \rightarrow 0$$

TYPE IIB STRING theory
on $AdS_5(R) \times S^5(R)$ space

- Coupling constant g_s
- R curvature radius
- $\sqrt{\alpha'}$ length of the string

Supergravity limit

$$g_s \rightarrow 0 \text{ e } R^2/\alpha' \rightarrow \infty$$

Maldacena

SYM/SUGRA DICTIONARY (Gubser, Klebanov, Polyakov, Witten)

Gauge-invariant p -form with conformal dimension Δ

Bulk field with mass m_5 given by $m_5^2 R^2 = (\Delta - p)(\Delta + p - 4)$

To describe hybrid $J^{PC}=1^{-+}$ mesons, we use the QCD local operator

$$J_\mu^a = \bar{q} T^a G_{\mu\nu} \gamma^\nu q \quad \mu, \nu = 0, 1, 2, 3$$

with $G_{\mu\nu}$ the gluon field strength and T^a flavour matrices normalised to $\text{Tr}[T^a T^b] = \delta^{ab}/2$. The dual field is a 1-form

$$H_M = H_M^a T^a \quad M = 0, 1, 2, 3, 4$$

whose dynamics is described by the action

$$S_{SUGRA} = \frac{1}{k} \int d^4 x \int_0^\infty dz \sqrt{|g|} e^{-c^2 z^2} \text{Tr} \left[-\frac{1}{4} F^{MN} F_{MN} + \frac{1}{2} m_5^2 H_M H^M \right]$$

with $F_{MN} = \partial_M H_N - \partial_N H_M$ and g determinant of the Poincaré metric

$$ds^2|_{AdS_5} = \frac{R^2}{z^2} (dt^2 - d\vec{x}^2 - dz^2), \quad z > 0$$

The Soft-Wall factor $e^{-c^2 z^2}$ gives the infrared conformal symmetry breaking through the mass scale c .

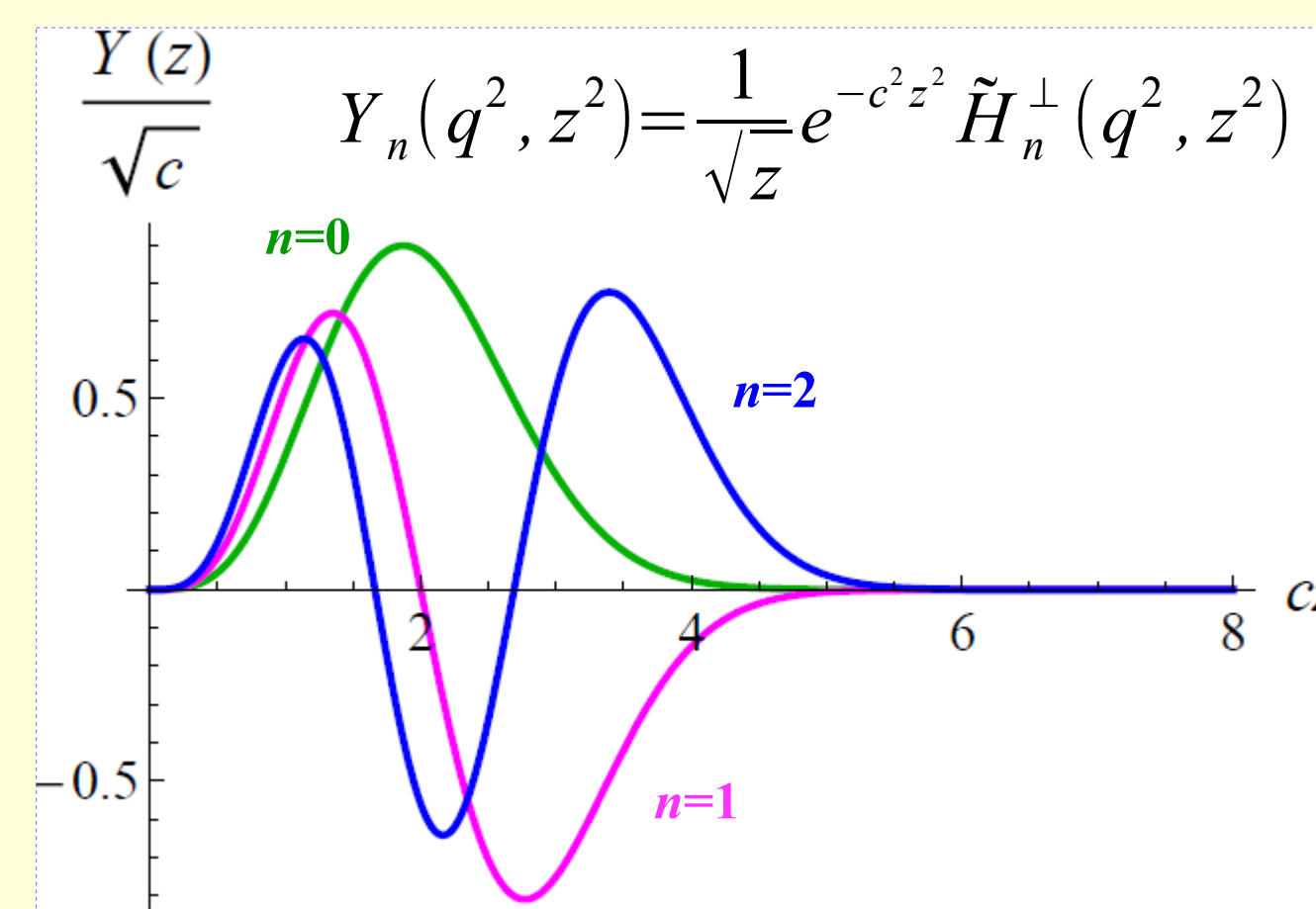
Mass Spectrum and Decay Constants

In the Fourier space the \tilde{H}_μ field can be decomposed in a longitudinal \tilde{H}_μ^\parallel , and in a transverse \tilde{H}_μ^\perp component; the latter satisfies the condition $q^\mu \tilde{H}_\mu^\perp = 0$ and can be used to describe the 1^{-+} mesons.

The equation of motion for \tilde{H}_μ^\perp is

$$\partial_z \left[\frac{1}{z} e^{-c^2 z^2} \partial_z \tilde{H}_\mu^\perp \right] + \frac{1}{z} e^{-c^2 z^2} q^2 \tilde{H}_\mu^\perp - \frac{8}{z^3} e^{-c^2 z^2} \tilde{H}_\mu^\perp = 0$$

EIGENFUNCTIONS



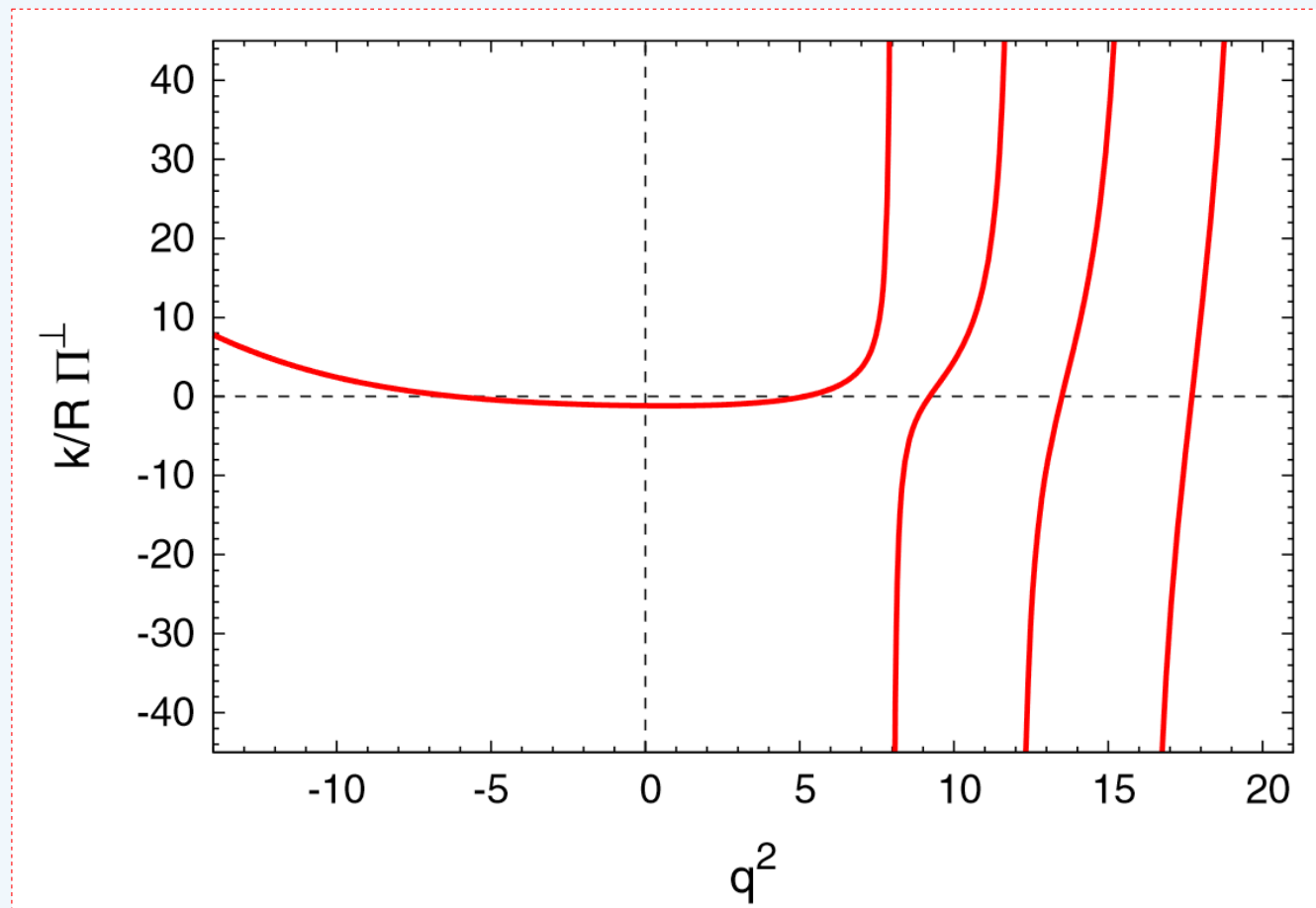
The Soft Wall model produces a 1^{-+} spectrum with a linear Regge trajectory $M_n^2 \approx n$ having the same slope as for other bound states with different quantum numbers and quark content.

J^{PC}	M_n^2
$1^{-+}(\bar{q}q)$	$c^2(4n+4)$
$0^{++}(\bar{q}q)$	$c^2(4n+6)$
$0^{++}(\text{glueball})$	$c^2(4n+8)$
$1^{-+}(\bar{q}Gq)$	$c^2(4n+8)$

For the lowest-lying state we find $M_0 \approx 1.1-1.3$ GeV, depending on the criterion chosen for fixing the mass scale c . The mass of the radial excitations grows more slowly than in the Hard Wall model, where $M_n^2 \approx n^2$.

The two-point correlation function in the Fourier space can be expressed as the sum of a transverse and a longitudinal contribution:

$$\Pi_{\mu\nu}^{ab}(q) = - \left(\eta_{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right) \frac{\delta^{ab}}{2} \Pi^\perp(q^2) + \frac{q_\mu q_\nu}{q^2} \frac{\delta^{ab}}{2} \Pi^\parallel(q^2)$$



The poles of $\Pi^\perp(q^2)$ reproduce the mass spectrum $M_n^2 = c^2(4n+8)$ with residues

$$F_n^2 = \frac{2Rc^8}{3k} (n+3)(n+2)(n+1)$$

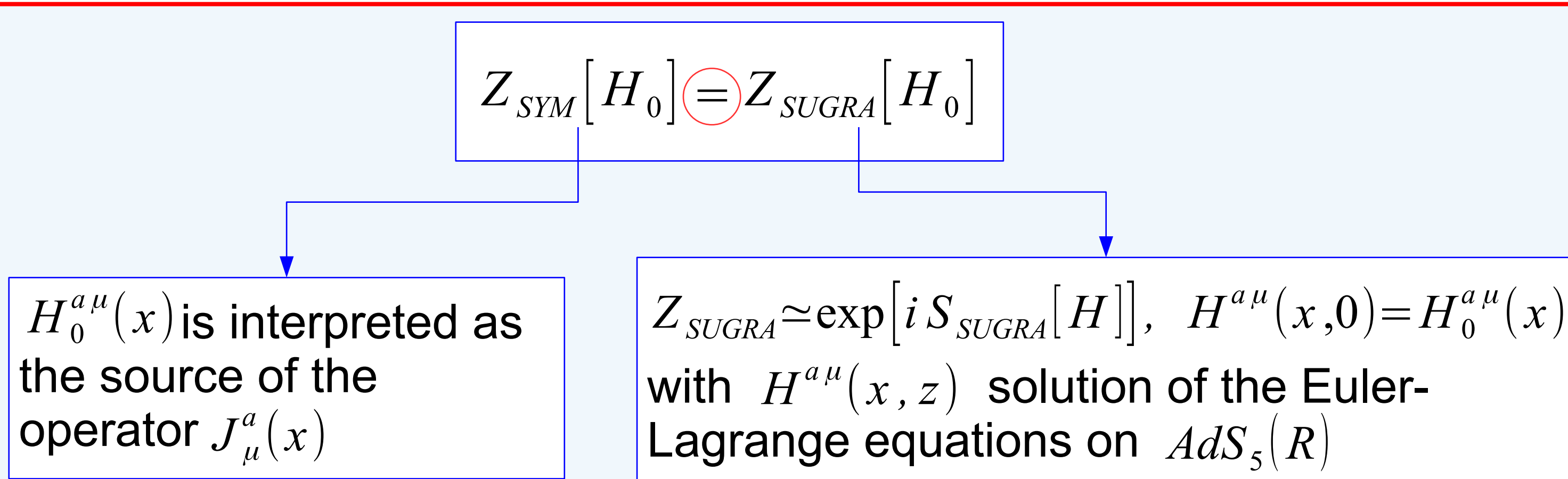
The ratio $R/k = 2/(5\pi^4)$ is fixed by matching the leading-order perturbative QCD expression for $\Pi^\perp(q^2)$ at $q^2 \rightarrow \infty$.

Stability against thermal effects

Temperature can be incorporated in the holographic models introducing a black hole in the $AdS_5(R)$ space

$$ds^2 = \frac{R^2}{z^2} \left(f(z) dt^2 - d\vec{x}^2 - \frac{dz^2}{f(z)} \right), \quad f(z) = 1 - \frac{z^4}{z_h^4}$$

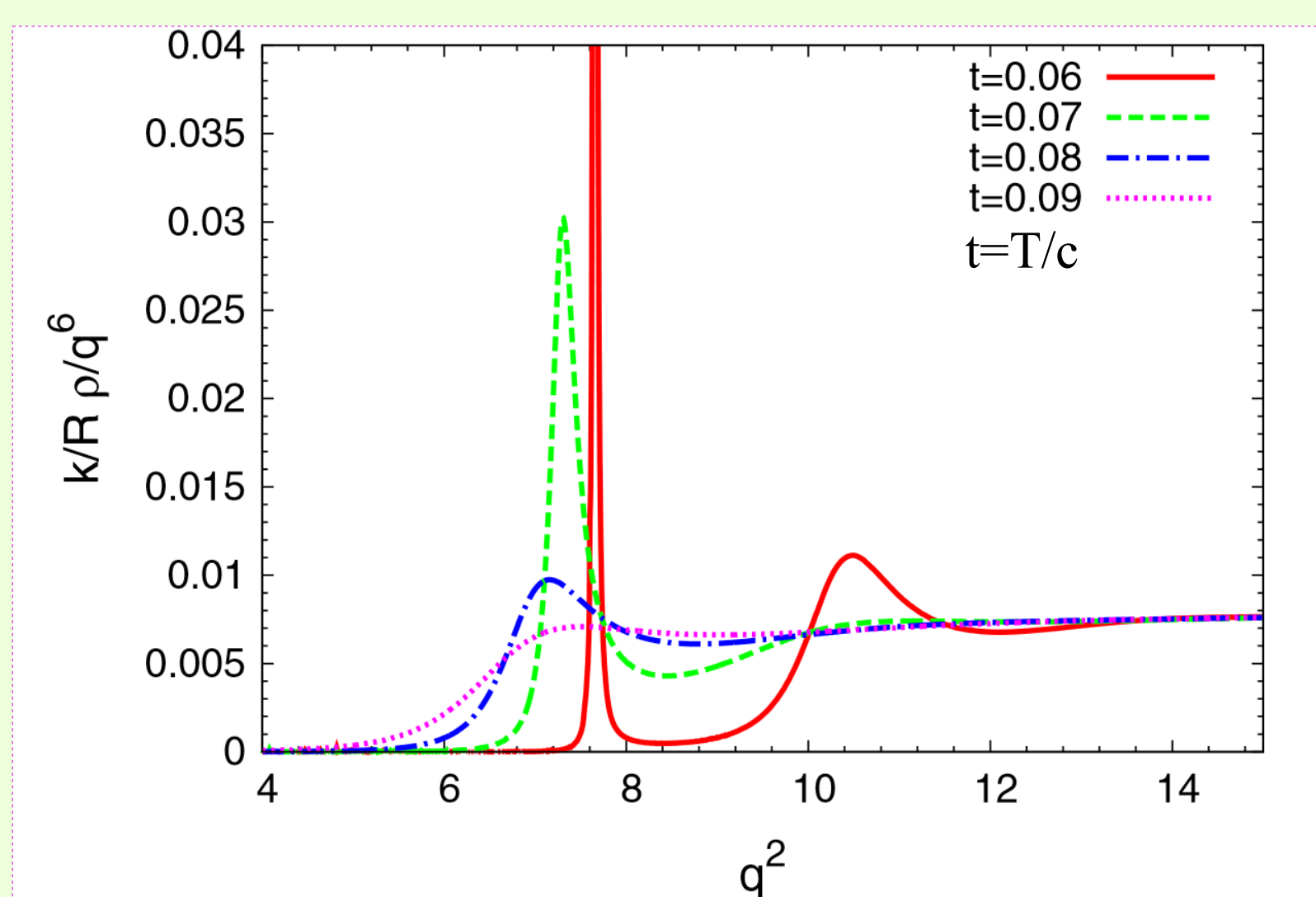
with the horizon position related to the inverse temperature by $z_h = 1/(\pi T)$.



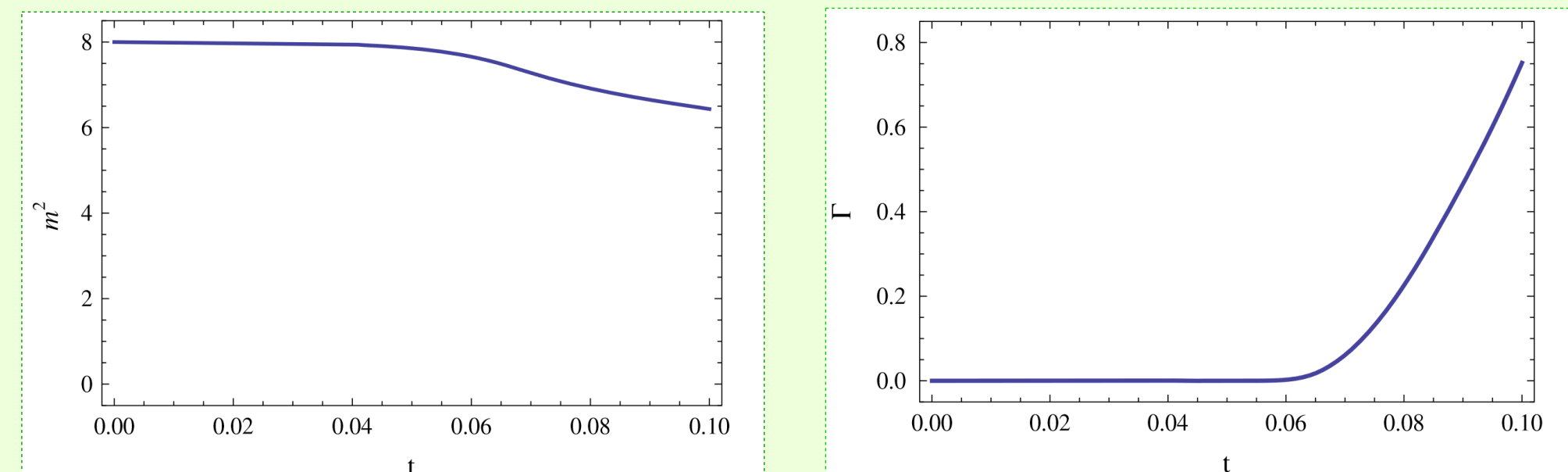
Two-point correlation function

$$\Pi_{\mu\nu}^{ab}(x-y) = \langle J_\mu^a(x) J_\nu^b(y) \rangle = \frac{1}{Z_{SYM}[0]} \left(-i \frac{\delta}{\delta H_0^{a\mu}(x)} \right) \left(-i \frac{\delta}{\delta H_0^{b\nu}(y)} \right) Z_{SYM}[H_0] \Big|_{H_0=0} = \frac{\delta^2 (S_{SUGRA})_{\text{on shell}}}{\delta H_0^{a\mu}(x) \delta H_0^{b\nu}(y)} \Big|_{H_0=0}$$

Spectral function $\rho(q^2) = \text{Im} \Pi^\perp(q^2)$



Squared mass m^2 and width Γ of the lightest 1^{-+} meson at increasing temperature (with $c=1$)



At the **melting temperature** the peak in the spectral function is reduced by a factor $\simeq 20$ with respect to the point where Γ starts to broaden.

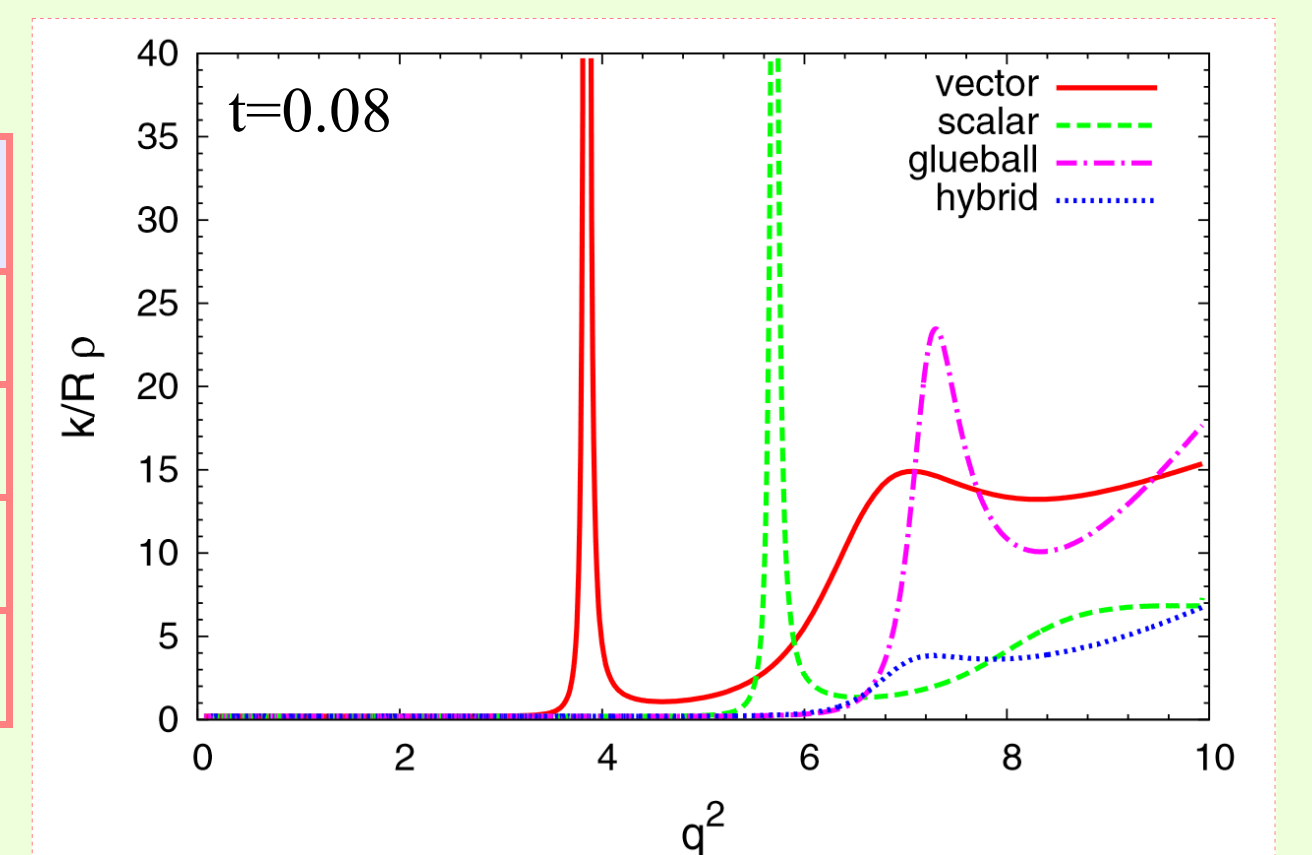
The **melting temperature** of the hybrid mesons can also be determined computing the **binding potential** in the Schrödinger-like equation for the transverse field $\tilde{H}_i^\perp(z, q)$

$$V(z) = \frac{f(z)}{z^2} \left(c^4 z^4 f(z) + \frac{4c^2 z^6}{z_h^4} + \frac{35}{4} + \frac{5z^4}{4z_h^4} \right), \quad \partial_r = -f(z) \partial_z$$

depending on the temperature through the horizon position. Below the melting temperature, the r -dependence of the potential becomes monotonous, such that no quasi-bound states can be formed.

RESPONSE TO TEMPERATURE OF BOUND STATES

J^{PC}	t_{melting}
$1^{-+}(\bar{q}q)$	0.23
$0^{++}(\bar{q}q)$	0.18
$0^{++}(\text{glueball})$	0.12
$1^{-+}(\bar{q}Gq)$	0.10



HYBRID MESONS MELT AT A LOWER TEMPERATURE!

